

9) 0.60 kg mass; vibrates 3.0 times/s; amplitude of 0.13 m

a) velocity @ eq = 2.48 m/s

b) velocity 0.10 m from eq = 1.56 m/s

c) total energy of system = 1.85 J

d) equation describing the motion of the mass, assuming  $x_{max}$  @  $t=0$  = ~~A~~

Find  $k$   $T = 2\pi \sqrt{m/k}$   $\frac{T}{2\pi} = \sqrt{m/k}$   $\frac{T^2}{4\pi^2} = m/k$   
 $k(T^2/4\pi^2) = m$   $k = m / T^2/4\pi^2 = k = \frac{4\pi^2 m}{T^2}$

$k = \frac{4\pi^2 (0.60 \text{ kg})}{0.33 \text{ s}^2} \rightarrow \boxed{217.51}$

$v_{max} = A \sqrt{k/m} \rightarrow v_{max} = 0.13 \text{ m} \sqrt{217.51 / 0.60 \text{ kg}}$   
 $= 2.48$

$E = \frac{1}{2} m v_{max}^2 \rightarrow E = \frac{1}{2} (.60 \text{ kg}) (2.48)^2$   
 $= 1.85 \text{ J}$

$v = \sqrt{\frac{kA^2 - kx^2}{m}}$   $v = \sqrt{\frac{(217.51)(.13 \text{ m})^2 - (217.51)(.10 \text{ m})^2}{0.60}}$   
 $E =$   
 $= 5.00$

$E = \frac{1}{2} kx^2 + \frac{1}{2} m v^2 = \frac{1}{2} (217.51)(.13^2) + \frac{1}{2} (.60 \text{ kg}) (2.48)^2$   
 $= 3.68$

$v = v_{max} \sqrt{1 - \frac{x^2}{A^2}} = 2.48 \sqrt{1 - \frac{.10^2}{.13^2}} = 1.58$

~~A~~ (d)  $x = A \cos(\omega t)$  ?  
 $x = (.13) \cos(2\pi(3)t)$

10) @ What displacement from eq is the speed of a SHO half the max value?

$$\frac{1}{2}kA^2 = \frac{1}{2}m\left(\frac{v_{\max}}{2}\right)^2 + \frac{1}{2}kx^2 \quad v_{\max} = A\sqrt{\frac{k}{m}}$$

$$\frac{1}{2}kA^2 = \frac{1}{2}m\left(\frac{A\sqrt{k/m}}{2}\right)^2 + \frac{1}{2}kx^2$$

$$\frac{1}{2}kA^2 = \frac{1}{2}m\left(\frac{kA^2}{4m}\right) + \frac{1}{2}kx^2$$

$$\cdot 8 \cdot \frac{1}{2}kA^2 = \frac{kA^2}{8} + \frac{1}{2}kx^2 \quad \cdot 8$$

$$4kA^2 = kA^2 + 4kx^2$$

$$-kA^2 \quad -4kx^2$$

$$\frac{3kA^2}{4k} = \frac{4kx^2}{4k}$$

$$\frac{3}{4}A^2 = x^2$$

$$x = \sqrt{\frac{3}{4}}A$$